

## NAG C Library Function Document

### nag\_zsytri (f07nwc)

#### 1 Purpose

nag\_zsytri (f07nwc) computes the inverse of a complex symmetric matrix  $A$ , where  $A$  has been factorized by nag\_zsytrf (f07nrc).

#### 2 Specification

```
void nag_zsytri (Nag_OrderType order, Nag_UploType uplo, Integer n, Complex a[],
                Integer pda, const Integer ipiv[], NagError *fail)
```

#### 3 Description

To compute the inverse of a complex symmetric matrix  $A$ , this function must be preceded by a call to nag\_zsytrf (f07nrc), which computes the Bunch–Kaufman factorization of  $A$ .

If **uplo** = **Nag\_Upper**,  $A = PUDU^T P^T$  and  $A^{-1}$  is computed by solving  $U^T P^T XPU = D^{-1}$  for  $X$ .

If **uplo** = **Nag\_Lower**,  $A = PLDL^T P^T$  and  $A^{-1}$  is computed by solving  $L^T P^T XPL = D^{-1}$  for  $X$ .

#### 4 References

Du Croz J J and Higham N J (1992) Stability of methods for matrix inversion *IMA J. Numer. Anal.* **12** 1–19

#### 5 Parameters

- 1: **order** – Nag\_OrderType *Input*  
*On entry:* the **order** parameter specifies the two-dimensional storage scheme being used, i.e., row-major ordering or column-major ordering. C language defined storage is specified by **order** = **Nag\_RowMajor**. See Section 2.2.1.4 of the Essential Introduction for a more detailed explanation of the use of this parameter.  
*Constraint:* **order** = **Nag\_RowMajor** or **Nag\_ColMajor**.
- 2: **uplo** – Nag\_UploType *Input*  
*On entry:* indicates how  $A$  has been factorized as follows:  
     if **uplo** = **Nag\_Upper**,  $A = PUDU^T P^T$ , where  $U$  is upper triangular;  
     if **uplo** = **Nag\_Lower**,  $A = PLDL^T P^T$ , where  $L$  is lower triangular.  
*Constraint:* **uplo** = **Nag\_Upper** or **Nag\_Lower**.
- 3: **n** – Integer *Input*  
*On entry:*  $n$ , the order of the matrix  $A$ .  
*Constraint:*  $n \geq 0$ .
- 4: **a**[*dim*] – Complex *Input/Output*  
**Note:** the dimension, *dim*, of the array **a** must be at least  $\max(1, \mathbf{pda} \times \mathbf{n})$ .  
*On entry:* details of the factorization of  $A$ , as returned by nag\_zsytrf (f07nrc).

*On exit:* the factorization is overwritten by the  $n$  by  $n$  symmetric matrix  $A^{-1}$ . If **uplo** = **Nag\_Upper**, the upper triangle of  $A^{-1}$  is stored in the upper triangular part of the array; if **uplo** = **Nag\_Lower**, the lower triangle of  $A^{-1}$  is stored in the lower triangular part of the array.

5: **pda** – Integer *Input*

*On entry:* the stride separating row or column elements (depending on the value of **order**) of the matrix in the array **a**.

*Constraint:* **pda**  $\geq \max(1, \mathbf{n})$ .

6: **ipiv**[*dim*] – const Integer *Input*

**Note:** the dimension, *dim*, of the array **ipiv** must be at least  $\max(1, \mathbf{n})$ .

*On entry:* details of the interchanges and the block structure of  $D$ , as returned by nag\_zsytrf (f07nrc).

7: **fail** – NagError \* *Output*

The NAG error parameter (see the Essential Introduction).

## 6 Error Indicators and Warnings

### NE\_INT

*On entry,* **n** =  $\langle value \rangle$ .

*Constraint:* **n**  $\geq 0$ .

*On entry,* **pda** =  $\langle value \rangle$ .

*Constraint:* **pda**  $> 0$ .

### NE\_INT\_2

*On entry,* **pda** =  $\langle value \rangle$ , **n** =  $\langle value \rangle$ .

*Constraint:* **pda**  $\geq \max(1, \mathbf{n})$ .

### NE\_SINGULAR

The block diagonal matrix  $D$  is exactly singular.

### NE\_ALLOC\_FAIL

Memory allocation failed.

### NE\_BAD\_PARAM

*On entry,* parameter  $\langle value \rangle$  had an illegal value.

### NE\_INTERNAL\_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please consult NAG for assistance.

## 7 Accuracy

The computed inverse  $X$  satisfies a bound of the form

if **uplo** = **Nag\_Upper**,  $|DU^T P^T X P U - I| \leq c(n)\epsilon(|D| |U^T| P^T |X| P |U| + |D| |D^{-1}|)$ ;

if **uplo** = **Nag\_Lower**,  $|DL^T P^T X P L - I| \leq c(n)\epsilon(|D| |L^T| P^T |X| P |L| + |D| |D^{-1}|)$ ,

$c(n)$  is a modest linear function of  $n$ , and  $\epsilon$  is the *machine precision*.

## 8 Further Comments

The total number of real floating-point operations is approximately  $\frac{8}{3}n^3$ .

The real analogue of this function is `nag_dsytri` (f07mjc).

## 9 Example

To compute the inverse of the matrix  $A$ , where

$$A = \begin{pmatrix} -0.39 - 0.71i & 5.14 - 0.64i & -7.86 - 2.96i & 3.80 + 0.92i \\ 5.14 - 0.64i & 8.86 + 1.81i & -3.52 + 0.58i & 5.32 - 1.59i \\ -7.86 - 2.96i & -3.52 + 0.58i & -2.83 - 0.03i & -1.54 - 2.86i \\ 3.80 + 0.92i & 5.32 - 1.59i & -1.54 - 2.86i & -0.56 + 0.12i \end{pmatrix}.$$

Here  $A$  is symmetric and must first be factorized by `nag_zsytrf` (f07nrc).

### 9.1 Program Text

```

/* nag_zsytri (f07nwc) Example Program.
 *
 * Copyright 2001 Numerical Algorithms Group.
 *
 * Mark 7, 2001.
 */

#include <stdio.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagf07.h>
#include <nagx04.h>

int main(void)
{
    /* Scalars */
    Integer i, j, n, pda;
    Integer exit_status=0;
    NagError fail;
    Nag_UploType uplo_enum;
    Nag_MatrixType matrix;
    Nag_OrderType order;
    /* Arrays */
    Integer *ipiv=0;
    char uplo[2];
    Complex *a=0;

#ifdef NAG_COLUMN_MAJOR
#define A(I,J) a[(J-1)*pda + I - 1]
    order = Nag_ColMajor;
#else
#define A(I,J) a[(I-1)*pda + J - 1]
    order = Nag_RowMajor;
#endif

    INIT_FAIL(fail);
    Vprintf("f07nwc Example Program Results\n\n");

    /* Skip heading in data file */
    Vscanf("%*[^\\n] ");
    Vscanf("%ld%*[^\\n] ", &n);
#ifdef NAG_COLUMN_MAJOR
    pda = n;
#else
    pda = n;
#endif
    /* Allocate memory */
    if ( !(ipiv = NAG_ALLOC(n, Integer)) ||

```

```

    !(a = NAG_ALLOC(n * n, Complex)) )
{
    Vprintf("Allocation failure\n");
    exit_status = -1;
    goto END;
}

/* Read A from data file */
Vscanf(" ' %1s '%*[\n] ", uplo);
if (*(unsigned char *)uplo == 'L')
{
    uplo_enum = Nag_Lower;
    matrix = Nag_LowerMatrix;
}
else if (*(unsigned char *)uplo == 'U')
{
    uplo_enum = Nag_Upper;
    matrix = Nag_UpperMatrix;
}
else
{
    Vprintf("Unrecognised character for Nag_UploType type\n");
    exit_status = -1;
    goto END;
}

if (uplo_enum == Nag_Upper)
{
    for (i = 1; i <= n; ++i)
    {
        for (j = i; j <= n; ++j)
            Vscanf(" ( %lf , %lf )", &A(i,j).re, &A(i,j).im);
        Vscanf("%*[\n] ");
    }
}
else
{
    for (i = 1; i <= n; ++i)
    {
        for (j = 1; j <= i; ++j)
            Vscanf(" ( %lf , %lf )", &A(i,j).re, &A(i,j).im);
        Vscanf("%*[\n] ");
    }
}

/* Factorize A */
f07nrc(order, uplo_enum, n, a, pda, ipiv, &fail);
if (fail.code != NE_NOERROR)
{
    Vprintf("Error from f07nrc.\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}

/* Compute inverse of A */
f07nwc(order, uplo_enum, n, a, pda, ipiv, &fail);
if (fail.code != NE_NOERROR)
{
    Vprintf("Error from f07nwc.\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}

/* Print inverse */
x04dbc(order, matrix, Nag_NonUnitDiag, n, n, a, pda, Nag_BracketForm,
        "%7.4f", "Inverse", Nag_IntegerLabels, 0,
        Nag_IntegerLabels, 0, 80, 0, 0, &fail);
if (fail.code != NE_NOERROR)
{
    Vprintf("Error from x04dbc.\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}

```

```

END:
  if (ipiv) NAG_FREE(ipiv);
  if (a) NAG_FREE(a);
  return exit_status;
}

```

## 9.2 Program Data

f07nwc Example Program Data

```

4                                     :Value of N
'L'                                   :Value of UPLO
(-0.39,-0.71)
( 5.14,-0.64) ( 8.86, 1.81)
(-7.86,-2.96) (-3.52, 0.58) (-2.83,-0.03)
( 3.80, 0.92) ( 5.32,-1.59) (-1.54,-2.86) (-0.56, 0.12) :End of matrix A

```

## 9.3 Program Results

f07nwc Example Program Results

```

Inverse
          1                2                3                4
1  (-0.1562,-0.1014)
2  ( 0.0400, 0.1527) ( 0.0946,-0.1475)
3  ( 0.0550, 0.0845) (-0.0326,-0.1370) (-0.1320,-0.0102)
4  ( 0.2162,-0.0742) (-0.0995,-0.0461) (-0.1793, 0.1183) (-0.2269, 0.2383)

```

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